## CC INTEGRATED || ETOOLS T

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## General Tools

## Algebra Tiles (CPM)

This tutorial describes how to use the Algebra Tiles including additional features.

## Click on the link below to access eTool.

## Algebra Tiles (CPM)

## 1. The top bar has three main parts: Pen \& Paper Icon, '?' Icon, and the Arrow Icon.

1. Select the Pen \& Paper Icon to:

Options - Add Title and Description and Enable/Disable Tools.
Clear Tiles - This will remove all the tiles that are in the tile area.
Save - This will save all the changes made.
2. Select the '?' icon for directions.
3. Select the Arrow Icon at the right to open and close the tray.


## 2. Drag tiles from the tray at the left to the display area at the right.

1. Select one of the tiles and drag it to the tile area.
2. Use the sliders in the tray to change the size of the tiles.
3. Double click tiles to change orientation (horizontal/vertical).
4. Click on a tile once to change the sign (+ -).

Note: The color of the tile will turn to red for negative sign.


## 3. Choose from a variety of different mats. Also choose from a variety of sizes to fit on various devices.

|  | No Background |  |  |
| :---: | :---: | :---: | :---: |
|  | Grid |  |  |
|  | Dot Grid |  |  |
|  | Expression Mat |  |  |
| $=$ | Equation Mat 1 |  |  |
|  | Equation Mat 2 |  |  |
| ? | Comparison Mat 1 |  |  |
|  | Comparison Mat 2 |  |  |
|  | Cornerpiece |  |  |
| Fit | Phone | S. Tablet | Tablet |

## 4. Choose from a variety of different tiles:

- Click the arrow next to the tool to view/hide the options for each tool.


## Pattern Tile \& Dot Tool (CPM)

## Click on the link below.

## Pattern Tile \& Dot Tool

## 1. Drag tiles from the tray to the Display area.

- Add tiles and copy and paste them to the display area.
- Select all tiles and drag to the tray to remove the tiles.



## 2. Textboxes and Dots

- Located in the General Tools
- Drag out and choose border/no border and color.
- Double click to rotate.
- Click to add text.


## (E)? CPM Tiles

Pattern Tiles \& Dot eTool

1. Use the square below for tiles.
2. Use the dot in the General Tools for dots.
3. Right Click or tap hold for color options.
4. Copy and paste for large number of tiles and dots.
5. Select all and drag to this tray to remove.
6. Select and drag to the mat textboxes in the General Tools menu to use as labels.
7. SAVE your work by copying and pasting the URL found in the Penci//Paper icon above to a doc or spreadsheet.


## Similarity Toolkit (CPM)

The similarity toolkit allows students to explore two triangles to determine congruency or similarity given SSS, SSA, SAS, AAA, etc.. Students show how two triangles are similar or congruent using rigid transformations (translation, rotation, and reflexion).

1. Click on the "Similarity Toolkit" link below. For additional help, click on the "Similarity Toolkit Video".

Similarity Toolkit Video
Similarity Toolkit (CPM)

## 2. Similarity Toolkit Basic Controls:


3. Indicate what sides/angles are similar/congruent.

4. By going to the Advanced Settings, indicate what angles and sides you want shown!


## Probability Tools (CPM)

## Click on the link below.

## Probability Tools (CPM)

## 1. Spinners:

- Drag one or more spinners to the board.
- Resize the spinners.
- Choose color, number of sections, and labels.
- Hide subdivisions.
- Create Mystery Spinners.
- Click the spinners to spin.



## 2. Dice:

- Drag one or more dice to the board.
- Choose dice color.
- Redesign the die with a variety of color, dot numbers, or Arabic numbers.
- Click each die to spin.



## 3. Bag:

- Drag one or more bags to the board.
- Choose the number, shape, and color of bag contents.
- Choose with or without replacement.
- Choose the number of items to draw.
- When finished, click the bad to shake and draw.



## 4. Coins:

- Coins are labelled "H" for Heads and "T" for Tails.
- Choose the color.
- Drag one or more coins to the board.
- Click each of them to spin.


## H

## H

## 5. Standard Deck of Cards:

- Drag one or more decks to the board.
- Choose with or without replacement and the number of cards draw at once.
- Modify the deck by eliminating specific cards or entire suits or number.
- Click the deck to draw the cards.



## 6. Random Number Generator:

- Drag the random number generator to the board.
- Indicate the number of integers to generate.
- Indicate the range for each random number.
- Click to randomize.



## Desmos Graphing Calculator

This free graphing calculator allows students to create a free account to save all of their graphs, animations, and projects created.

Click on the "Desmos Graphing Calculator" link below.
Desmos Graphing Calculator

1. Click on all of the buttons. Try it out! For extra help, click the "?".

2. Click on the interactive tours below for help to create:

Sliders
Tables
Advanced Tables
Restrictions

## 3. The interactive tours will NOT let you make a mistake! Try the links above!

Interactive Tours<br>Team Desmos<br>posted this on December 29, 2013 22:13

Try one (or alll) of the interactive tours to learn more about sliders, tables, restrictions, and more:


## 4. Need additional help? Watch these very short excellent videos!

Desmos Introduction
Moveable Points
Graph Inequalities
Piece-Wise Function
5. The video links will help you with many of your graphing projects!


## 6. If you still need help, check out Desmos "Knowledge Base"

 Desmos Knowledge Base
## Polygon Bucket eTool (Desmos)

## Click on the link below to access eTool.

## Polygon Bucket (Desmos)

## Use this eTool to explore polygons.

- To move a shape, click the colored dot and drag the shape to where you want to move it.
- To hide/show a shape, click the folder icon before the name of the shape.



## Polygon Bucket and Venn Diagram Practice eTool (Desmos)

## Click on the link below to access eTool.

## Polygon Bucket (Desmos)

## Use this eTool to learn more about different Polygons and Venn Diagram.

1. Move a shape to the appropriate section on the Venn Diagram.

- Click the colored dot and drag it to the appropriate section on the Venn Diagram

2. Click the folder icon before the name of the shape to view or hide a shape.


## Table Tool (CPM)

## Click on the link below to access the eTool.

## CPM Table eTool

## 1. CPM Table eTool

- Find patterns
- Highlight cells
- Highlight rows

| Table Q 2016 CPM Educational Program. Al rights reserved. |  |  |  |  |  |  |  |  |  |  |  | Directions |  | Reset | Save |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 |  |
| 1 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 |
| 2 | 2 | 4 | 6 | 8 | 10 | 12 | 14 | 16 | 18 | 20 | 22 | 24 | 26 | 28 | 30 |
| 3 | 3 | 6 | 9 | 12 | 15 | 18 | 21 | 24 | 27 | 30 | 33 | 36 | 39 | 42 | 45 |
| 4 | 4 | 8 | 12 | 16 | 20 | 24 | 28 | 32 | 36 | 40 | 44 | 48 | 52 | 56 | 60 |
| 5 | 5 | 10 | 15 | 20 | 25 | 30 | 35 | 40 | 45 | 50 | 55 | 60 | 65 | 70 | 75 |
| 6 | 6 | 12 | 18 | 24 | 30 | 36 | 42 | 48 | 54 | 60 | 66 | 72 | 78 | 84 | 90 |
| 7 | 7 | 14 | 21 | 28 | 35 | 42 | 49 | 56 | 63 | 70 | 77 | 84 | 91 | 98 | 105 |
| 8 | 8 | 16 | 24 | 32 | 40 | 48 | 56 | 64 | 72 | 80 | 88 | 96 | 104 | 112 | 120 |
| 9 | 9 | 18 | 27 | 36 | 45 | 54 | 63 | 72 | 81 | 90 | 99 | 108 | 117 | 126 | 135 |
| 10 | 10 | 20 | 30 | 40 | 50 | 60 | 70 | 80 | 90 | 100 | 110 | 120 | 130 | 140 | 150 |
| 11 | 11 | 22 | 33 | 44 | 55 | 66 | 77 | 88 | 99 | 110 | 121 | 132 | 143 | 154 | 165 |
| 12 | 12 | 24 | 36 | 48 | 60 | 72 | 84 | 96 | 108 | 120 | 132 | 144 | 156 | 168 | 180 |
| 13 | 13 | 26 | 39 | 52 | 65 | 78 | 91 | 104 | 117 | 130 | 143 | 156 | 169 | 182 | 195 |
| 14 | 14 | 28 | 42 | 56 | 70 | 84 | 98 | 112 | 126 | 140 | 154 | 168 | 182 | 196 | 210 |
| 15 | 15 | 30 | 45 | 60 | 75 | 90 | 105 | 120 | 135 | 150 | 165 | 180 | 195 | 210 | 225 |

## 2. Highlight

- Click on a row or column and highlight.
- Click on a cell and choose the color.

| 6 7 N | $\begin{aligned} & \mathbf{u} \\ & \mathbf{x} \end{aligned}$ |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Highlight column |  |  |  |  |  |  |  |  |  |  |
| Clear cell | Table <br> e 2016 CPM Educational Program. Al rights ruserved. |  |  |  |  |  |  |  |  |  |
|  |  | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
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|  | 2 | 2 | 4 | 6 | 8 | 10 | 12 | 14 | 16 | 18 |
|  | 3 | 3 | 6 | 9 | 12 | 15 | 18 | 21 | 24 | 27 |
|  | 4 | 4 | 8 | 12 | 16 | 20 | 24 | 28 | 32 | 36 |
|  | 5 | 5 | 10 | 15 | 20 | 25 | 30 | 35 | 40 | 45 |
|  | 6 | 6 | 12 | 18 | 24 | 30 | 36 | 42 | 48 | 54 |
|  | 7 | 7 | 14 | 21 | 28 | 35 | 42 | 49 | 56 | 63 |


| 3 | 4 | 5 | 6 | 7 | 8 | $\frac{0}{x}$ |
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| 3 | 4 | 5 |  |  |  |  |
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| 12 | 16 | 20 | : |  | Cle |  |
| 15 | 20 | 25 | 30 | 35 | 40 | 45 |
| 18 | 24 | 30 | 36 | 42 | 48 | 54 |
| 21 | 28 | 35 | 42 | 49 | 56 | 63 |

## Chapter 1

## INT2 1.1.1: Teacher Mobius Strip Setup, Lesson, \& Closure Video

Click on the links below for the "Mobius" videos
Möbius Strip Setup ${ }^{[-1}$
Möbius Strip classroom Lesson
Möbius Strip Closure $\qquad$

1. Materials Preparation:

2. Using the strips:

3. Predicting results:


## 4. Closure:



## INT2 1.1.1 1-3 Venn Diagrams Student eTools (Desmos)

## Click on the links below to access eTools.

## 1-3 Venn Diagram A: Student eTool(Desmos)

## 1-3 Venn Diagram B: Student eTool(Desmos)

1-3 Venn Diagram C: Student eTool(Desmos)

A Venn diagram is a tool used to classify objects. An item is placed in the Venn diagram in the appropriate region based on the conditions it meets.

## 1-3 Venn Diagram A

The left circle of the Venn diagram, Circle \#1, represents the condition "has at least one pair of parallel sides" and the right side, Circle \#2, represents the condition "has at least two sides of equal length" as shown below.

Sort through the polygons in the Polygon Bucket and decide as a team where each polygon belongs.

- Click on the colored points on each shape and drag it to the appropriate section on the Venn Diagram.



## 1-3 Venn Diagram B

Next, reclassify the polygons for the new Venn diagram shown below.

- Click on the colored points on each shape and drag it to the appropriate section on the Venn Diagram.



## 1-3 Venn Diagram C

Finally, reclassify the polygons for the new Venn diagram shown below.

- Click on the colored points on each shape and drag it to the appropriate section on the Venn Diagram.



## INT2: 1.1.1 1-3 Venn Diagrams Answer eTools (Desmos)

## Click on the links below to access eTools.

1-3 Venn Diagram A: Answer eTool(Desmos)
1-3 Venn Diagram B: Answer eTool(Desmos)
1-3 Venn Diagram C: Answer eTool(Desmos)

1-3 Venn Diagram A Answer


## 1-3 Venn Diagram B Answer



## 1-3 Venn Diagram C Answer



## INT2: 1.1.2 1-10 Student eTool (Desmos)

Click on the link below to access eTool.

## 1-10 Student eTool (Desmos)

## Use this eTool to learn more about different Polygons and Venn Diagram.

1. Move a shape to the appropriate section on the Venn Diagram.

- Click the colored dot and drag it to the appropriate section on the Venn Diagram

2. Click the folder icon before the name of the shape to view or hide a shape.


## INT2 1.2.1: 1-52 Venn Diagrams Shape A, B \& C eTools (Desmos)

## Click on the links below.

Shape Bucket(Desmos)
Generic Venn Diagram(Desmos)
1-52 Venn Diagram A: Student eTool(Desmos)
1-52 Venn Diagram B: Student eTool(Desmos)
1-52 Venn Diagram C: Student eTool(Desmos)

## 1. Shape Bucket



## 2. Generic Venn Diagram

- Type the attributes for each circle at the left
- Fill the circles appropriately.



## 3. Venn Diagram A:

- Hide the tray for more room to move the shapes.
- Enlarge/shrink the shapes by using the mouse or pinching on a tablet.



## 4. Venn Diagram B:

- Hide the tray for more room to move the shapes.
- Enlarge/shrink the shapes by using the mouse or pinching on a tablet.



## 5. Venn Diagram C:

- Hide the tray for more room to move the shapes.
- Enlarge/shrink the shapes by using the mouse or pinching on a tablet.



## INT2 1.2.1: 1-52 Venn Diagrams Shape A, B \& C Answer eTools

Click on the link below for the "Shape A, B \& C Answer eTools"
1-52 Venn Diagram A: Answer eTool
1-52 Venn Diagram B: Answer eTool
1-52 Venn Diagram C: Answer eTool

1. Venn Diagram Answer A: See below for the placement of shapes.

2. Venn Diagram Answer B: See below for the placement of shapes.

3. Venn Diagram Answer C: See below for the placement of shapes.


## INT2 1.3.2: Marcos' Tile Pattern (CPM)

Tessellate the parallelograms by sliding them up, down, or sideways. Double click the yellow parallelogram to rotate.

Click the link below.
Marcos' Tile Pattern (CPM)

This is an interactive eTool about Marcos's Tile Pattern.

1. Click on the yellow tile and drag it away from the blue tile.
```
E/? Marcos' Tile Pattern
    (4)16 CPM Educational Program.
    All rights reserved.
            Privacy Policy.
```


2. Click the blue tile and drag horizontally or vertically to tessellate.

3. Click and drag until the entire space is covered.


## 4. Double click on the yellow tile to rotate at $\mathbf{9 0}$ degree intervals.



## INT2 1.3.2: Reflection of Light Teacher Demonstration

Click on the link below for the "Reflection of Light Demonstration"
Reflection of Light Demonstration

1. The laser is pointing at the mirror on the chalk board tray.

2. The laser and chalk dust show the reflection of the laser beam.


## INT2 1.3.4: Triangle Sum Theorem (Desmos)

## Click on the link below to access eTool.

## Triangle Sum Theorem (Desmos)

## 1. Triangle Sum Theorem:

- Click the points and drag to change the angles.

NOTE: The Sum and values of round (A) to (C) change when the points are moved.

2. How does "Show Parallel Lines" help when determining the sum of the interior angles of a triangle?

- Click the folder icon in Line for to show the Parallel Lines.



## INT2 1.3.4: Triangle Inequality eTool (Desmos)

## Click on the link below to access eTool.

Triangle Inequality eTool (Desmos)

## Use this eTool to determine the length of the third side of a triangle if the length of the two other sides are given.

1. Adjust the the side lengths of the triangles.

- Click the blue points (horizontally) on the sliders and drag it to the desired length.

2. Move the two points $B$ to coincide.

- Click the points B one at a time and drag it to where they both coincide.



## Chapter 2

## INT2 2.1.1: Pantograph Teacher Video

Click on the link below.
Pantograph Teacher Video $\quad=$

1. Prepare the rubber bands:

2. Knot two rubber bands:

3. Several rubber bands strung together:

4. White board demonstration:


## 5. Student demonstration:



## INT2 2.1.2: Similarity Stretching Word Document (CPM)

This document will download to your computer.

Click on the link below for the "Similarity Stretching Word Document".
Similarity Stretching Word Document

## |

## STRETCHING EXERCISE



Original

## INT2 2.2.1: 2-33b, 2-33c, 2-35a, 2-35b\#1,\& 2-35b\#2 Student eTools

## Click on the links below.

2-33b Student eTool (CPM)
2-33c Student eTool (CPM)
2-35a Student eTool (CPM)
2-35b \#1 Student eTool (CPM)
2-35b \#2 Student eTool (CPM)

## 1. INT2 2-33b:



## 2. INT2 2-33c:

* ? CPM Similarity

INT2 2-33c

## $\nabla$ Notes

INT2 2-33c
c) Describe a sequence of transformations to show that two triangles that have the same show that two triangics

Transformations:
Transformations:
Drag triangles from the center to translate. Drag triangles from the center to translate.
Click on the center of a triangle to access the

- Show/Hide Labels
- Side Lengths and Ratios



## 3. INT2 2-35a:

## * ? CPM Similarity

2-35a Student eTool
$\nabla$ Notes
INT2 2-35a
Is it possible to make a second triangle with two sides proportional to 4 cm and 5 cm , and an included angle of $20^{\circ}$ that is not similar?

Note: A possible second triangle with sides 8 cm and 10 cm , and an included angle of $20^{\circ}$ is given for you to test.

- Show/Hide Labels
- Side Lengths and Ratios



## 4. INT2 2-35b \#1:

2-35b \#1 Student eTool
Votes
inT2 2-35b al
Is it possible to make a second triangle with
two sides proportional to 3 cm and 4 cm , and
an included angle of $120^{\circ}$ that is not similar?
Note: A possible second triangle with sides 6
cm and 8 cm , and an included angle of $120^{+}$is
given for you to test!
Show/Hide Labels
Side Lengths and Ratios


## 5. INT2 2-35b \#2:

## \% ? CPM Similarity

2-35b \#2 Student eTool

## Notes

iNT2 2-35b \#2
Is it possible to make a sccond triangle with two sides proportional to 3 cm and 4 cm , and an included angle of $90^{\circ}$ that is not similar?

Note: A possible second triangle with sides 6 cm and 8 cm , and an included angle of $90^{\circ}$ is given for you to test!

Show/Hide Labels
Side Lengths and Ratios


## INT2 2.2.2: 2-46b \#1, 2-46b \#2 eTool, \& 2-47 Student eTools

## Click on the links below.

2-46b \#1 eTool (CPM)
2-46b \#2 eTool (CPM)
2-47 Student eTool (CPM)

## 1. INT2 2-46b\#1



## 2. INT2 2-46b \#2



## 3. INT 2 2-47:

## * ? CPM Similarity

2-47 Student eTool
Notes
INT2 2-47
Transformations:
Drag triangles from the center to translate. Click on the center of a triangle to access the rotate, reflect, and dilate tools. Click on the "?" above for more directions.

Show/Hide Labels
Side Lengths and Ratios


## INT2 2.2.2: 2-47 Answer eTool

## Click on the link below.

2-47 Answer eTool (CPM)

## 2-47 Answer eTool

## Notes

## INT2 2-47 Answer

The smaller triangle has the sides 4 and 5 with an angle of 49 which is not similar to the larger triangle.

Transformations:
Drag triangles from the center to translate Click on the center of a triangle to access

Show/Hide Labels
Side Lengths and Ratios


## INT2 2.2.4: Squawk Like a Chicken Teacher Materials Setup

Click on the link below for the "Squawk Like a Chicken Materials Setup"
Squawk Like a Chicken Materials Setup
1.

2.

3.

4.

5.


## INT2 2.3.1: 2-85 Student eTool \& Leaning Tower of Pisa Video

Click on the link below for the "Leaning Tower of Pisa and Information Video"

2-85 Student eTool (Desmos)
Leaning Tower of Pisa Information Video

1. Estimate the angle the tower is leaning using the protractor.

2. This video shows the architecture of the Leaning Tower of Pisa.


## INT2 2.3.3: Slope Ratios

## Click on the link below for the "Slope Ratios" eTool.

## Slope Ratios (Desmos)

## 1. Use the sliders to:

- Select an angle.
- Change the length of the adjacent side, delta $x$.
- The opposite side length, delta y , and the slope are calculated below.



## INT2 2.3.5: Clinometer Teacher Videos

Click on the links below.

Clinometer Preparation ${ }^{2}$<br>Clinometer Lesson<br>$\qquad$<br>Study Team Work<br>Closure Lesson

1. Assemby:

2. More assembly:


## 3. Introduction:



4-42. HOW TALL IS IT?
How How tall is Mount Everest? How tall is the White House? Often we want to know a measurement of something we cannot easily measure with a ruler or tape measure. Today you will work with your team to measure the height of something inside your classroom or on your school's campus in order to apply your new tangent tool.
4. Collecting data:


## 5. Team discussion:



## CPM CPM Educational Program

## 6. Closure:



## INT2 2.3.5: History of the Statue of Liberty

Click on the link below for the "History of the Statue of Liberty"
History of the Statue of Liberty
1.

2.

3.

4.


## Chapter 3

## INT2 3.1.2: 3-12 Student eTool (CPM)

## Click on the link below to access eTool.

## 3-12 Student eTool (CPM)

## Use this eTool to play the spinner game.

- Click each spinner to select random letter.

Note: Spinner \#1 is for the first letter and Spinner \#2 is for the second letter.


## INT2 3.1.3: 3-24 Student eTool (CPM)

## Click on the link below to access eTool.

3-24 Student eTool (CPM)

## Pick a Tile Game

## * ? CPM Probability

INT2 3-24 Student eTool
There is a new game at the school fair called "Pick a Tile," in which the player reaches into two bags and chooses one square tile and one circular tile.

The bag with squares contains three yellow, one blue, and two red squares.

The bag with circles has one yellow and two red circles.

Choose one BLUE SQUARE and one RED CIRCLE to win.

## It costs $\$ 2$ to play.

- Probability Tools
- General Tools


## Click each bag to pick a square tile and a circle tile randomly.

Pick a Tile



## TI-84: Generating Random Numbers

1. Be sure you "seed" your calculator. This will ensure that the same random numbers do not appear on everyone's calculator. Enter a random number in the calculator such as the student ID number or telephone number. Then press [STO->] [MATH] "PRB" "1:rand".

Note: This step only needs to be completed once unless you reset the calculator! Â And you will not get the same numbers!

2. Specify the minimum and maximum integers possible, and how many random integers to generate. For example, [MATH] "PRB" "5:randInt(1,10,5)" [ENTER] generates 5 numbers between 1 and 10.

Note: Hit [Enter] to get 5 more random numbers between 1 and 10 . Of course, you will not likely get the same random numbers.
randint(1, 10,5)
$\left.\begin{array}{llll}5 & 10 & 5 & 6 \\ \hline\end{array}\right)$
randInt( $1,10,5$ )
$\left.\begin{array}{llll}3 & 1 & 8 & 5\end{array}\right)$
3. To simulate flipping a coin, let ' 0 ' be heads and ' 1 ' be tails. For example, [MATH] "PRB" "5:randInt( $0,1,6$ )" [ENTER] generates 6 numbers between 0 and 1. All of the ' 0 's are Heads. All of the ' 1 's are Tails!

The image below shows 3 heads and 3 tails. Then it shows 4 heads and 2 tails.

4. To simulate rolling dice, go to [MATH] "PRB" "5:randInt(1,6,2)" [ENTER] generates 2 numbers between 1 and 6.

The image below shows rolling a die three times and the results.

| T1-84 Plus Silver Edition <br> ti Texas Instruments <br> randInt( $1,6,2) 5$ randInt ( $1,6,2$ ) randInt ( $1,6,6$ ) <br> 13 |
| :---: |
|  |  |

5. You could also generate a lot of numbers and store them in a list. For example, [MATH] "PRB" "5:randInt(1,10,100" [ENTER] generates 100 numbers between 1 and 10. Then [STO->] [2nd] 'L1' will place the numbers in List 1.

| T1-84 Plus Silver Edition |
| :---: |
| Fris ${ }^{\text {L }}$ |
| 674812 |
| aridint (1,10,1 |
| 6576816 \% |
| Ans- $\mathrm{L}_{\text {\% }}$ |
| ¢3576816 |

## INT2 3-36 \& 3-43 Student eTools

## Click on the links below.

3-36 Student eTool (CPM)
3-43 Student eTool (CPM)

## 1. INT2 3-36 Student eTool:

- Click on the number box to generate a new random number
- The numbers will simulate numbers on a roulette wheel.
- " 00 " will be represented by a -1 on the random generator.


## INT2 3-36 Student eTool

Click the box at the right to generate a random number from $-1,0,1, \ldots, 36$.

The -1 will represent 00 on the roulette wheel.

Probability Tools
General Tools

## 2. INT2 3-43 Student eTool:

- Click the spinner to spin.


## INT2 3-43 Student eTool

Click the spinner at right to spin.
Probability Tools

- General Tools



## INT2 3.1.5: 3-47, 3-48, and 3-49 Student eTools (CPM)

## Click on the links below to access eTools.

3-47 Student eTool (CPM)
3-48 Student eTool (CPM)
3-49 Student eTool (CPM)

## Take A Spin Games

## 3-47: Take A Spin \#1

- Click on the wheel to spin.

| ? CPM Probability |
| :--- |
| INT2 3-47 Student eTool |
| 3-47. TAKE A SPIN |
| Consider the following game: After |
| clicking the wheel at right, you win |
| the amount spun. |
| a. If you play the game 10 times, how <br> much money would you expect to <br> win? What if you played the game 30 <br> times? 100 times? Explain your <br> process. <br> b. If you were to play only once, what <br> would you expect to earn according to <br> your answers in part (a)? Is it actually <br> possible to win that amount? Explain <br> why or why not. |
| Probability Tools |

3-48: Take A Spin \#2

- Click on the wheel to spin.



## 3-49: Take A Spin \#3

## - Click on the wheel to spin.

## * ? CPM Probability

INT2 3-49 Student eTool
3-49. Jesse has created the spinner at right. This time, if you land on a positive number, you win that amount of money. However, if you land on a negative number, you lose that amount of money! Want to try it?
a. Before analyzing the spinner predict whether a person would win money or lose money after many spins.
b. Now calculate the actual expected value. How does the result compare to your estimate from part (a)?
c. What would the expected value be if this spinner were fair? Discuss this with your team. What does it mean for a spinner to be fair?
d. How could you change the spinner to make it fair? Draw your new spinner and show why it is fair.

Take A Spin \#3


## INT2 3.1.5: 3-50, 3-51 \& 3-52 Spinners

Click on the links below.
3-50 Student eTool (CPM)
3-51 Student eTool (CPM)
3-52 Student eTool (CPM)

## 1. Int2 3-50 Student eTool:

INT2 3-50 Student eTool
Game Rules:
After clicking the wheel at right, you win the amount spun.
a. If you play the game 10 times, how much money would you expect to win? What if you played the game 30 times? 100 times? Explain your process.
b. What if you played the game n times? Write an equation for how much money someone can expect to win after playing the game n times.
c. If you were to play only once, what would you expect to earn according to your equation in part (b)? Is it actually possible to win that amount? Explain why or why not.


## 2. Int2 3-51 Student eTool:

INT2 3-51 Student eTool

## Game Rules:

Click the wheel to spin. Total your winnings from each spin.
a. If you win the amount that comes up on each spin, how much would you expect to win after 4 spins?
What about after 100 spins?
b. Find this spinner's expected value. That is, what is the expected amount you will win for each spin? Be ready to justify your answer.
c. Gustavo describes his thinking this way: "Half the time, I'll earn nothing. One-fourth the time, I'll earn $\$ 4$ and the other one-fourth of the time I'll earn $\$ 100$. So, for one spin, I can expect to win $.5(0)+$ $.25(\$ 4)+.25 \$ 100)$." Calculate Gustavo's expression. Does his result match your result from part (h)?

Take A Spin \#2


## 3. Int2 3-52 Student eTool:

*) ? CPM Probability
INT2 3-52 Student eTool
Jesse has created the spinner at right. This time, if you land on a positive number, you win that amount of money. However, if you land on a negative number, you lose that amount of money!
a. Before analyzing the spinner, predict whether a person would win money or lose money after many spins.
b. Now calculate the actual expected value. How does the result compare to your estimate from part (a)?
c. What would the expected value be if this spinner were fair? Discuss this with your team. What does it mean for a spinner to be fair?
d. How could you change the spinner to make it fair? Draw your new spinner and show why it is fair.

## INT2 3.2.3: 3-89 and 3-90 Student eTools (Desmos)

## Click on the links below to access eTools.

3-89 Student eTool (Desmos)
3-90 Student eTool (Desmos)

## Slope Ratios

3-89

- Click on the green point on the graph and drag it to increase the angle.


3-90

- Click on the green point on the graph and drag it to create trianlge.
- Click on the "+" and "-" on the upper right corner of the eTool to Zoom In and Zoom Out the graph.



## INT2 3.2.4: 3-106 Student eTool

## Click on the link below.

Int2 3-106 Student eTool (Desmos)

1. Move the slider to the desired angle. Use the diagram and your knowledge of trigonometry to solve the parts in this problem.


## INT2 3.2.4: 3-104 Teacher eTool \& 3-106 Answer eTool

## Click on the link below for the "3-106 Answer eTool".

3-104 Teacher eTool (Desmos)
3-106 Answer eTool (Desmos)

## 1. Int2 3-104 Teacher eTool

- Use as a closure activity.
- Students come to the board and discuss each part.



## 2. Int2 3-104 Teacher eTool:

- Click on each circle in font of each step to show the part in the diagram.
- Click on the arrows to show the calculations.
INT2 3-104 Teacher eTool

| Click the circles to view the |
| :--- |
| lengths on the graph. Click the |
| folder arrows to view the |
| calculations. |

(B) Show Rope to Carabiner
(B) Distance from base of cliff
(B) Show feet to ground
(B) Height to Emily's Waist

## 3. Int2 3-106 Answer eTool:

- Move the slider for the various desired angles.




## 4. Int2 3-106 Answer eTool:

- Click the folder arrows for answers to the various parts of this problem.



## Chapter 4

## INT2 4.1.2: 4-13a Student eTool (CPM)

## Click on the link below to access eTool.

## 4-13a Student eTool (CPM)

Use this eTool to build a rectangle from the given tiles for problem 4-13a.

- Click each tile and drag it to the desire location.



## Int2 4.2.2: 4-46a Student eTool (CPM)

## Click on the link below.

4-46a Student eTool (CPM)

## 4-46a Student eTool:

Int2 4-46a Student eTool

1. Go to the "?" above for additional help! Then go to pages $8 \& 9$.
2. Move the algebra tiles to form a rectangle.
3. Double click the " $x$ ' $s$ " to rotate them.

Backgrounds

- Algebra Tiles

Label:


## INT2 4.2.4: 4-89 Teacher eTool (Desmos)

## Click on the link below to access the eTool.

## 4-89 Teacher eTool (Desmos)

## Use this eTool to discuss problem 4-89.



1. Click the circle on the left to view/hide the lengths of the graph.

2. Click the arrows to view/hide the calculations in each folder.


## INT2 4.1.2: 4-91 Student eTool (Desmos)

## Click on the link below to access the eTool.

## 4-91 Student eTool (Desmos)

## Use this eTool to visualize problem 4-91.

- Click on the angle slider and drag (horizontally) to adjust the angle.



## INT2 4.2.4: 4-91 Answer eTool (Desmos)

Click on the link below to access eTool.
4-91 Answer eTool (Desmos)

4-91 Answer graph


## 1. Click the BLUE point (Angle slider) and drag (horizontally) to adjust the angle.

2. Click the arrow before parts (a), (b), and (c) to view/hide the folder content.


## Chapter 5

## INT2 5.1.2: 5-16 Student eTool (Desmos)

## Click on the link below to access eTool.

## 5-16 Student eTool (Desmos)

Use this eTool to complete part (a) of problem 5-16.


## 1. Click the arrow to the left of each contestant the view the folder content.

2. Enter the ' $x$ ' and ' $y$ 'values in each table.
3. Type in an equation below each table.
4. Click the circle to the left of each contestant to view their data.


## INT2 5.1.2: 5-16 Answer eTool (Desmos)

## Click on the link below to access eTool.

## 5-16 Answer eTool (Desmos)

## 5-16 Answer Graphs:



## 1. Click on the folder icon to hide/view contestan's graph.

2. Click the arrow to the left of each contestant to view/hide the folder content.


## INT2 5.2.3: 5-83 Student eTool (CPM)

## Click on the link below to access eTool.

## 5-83 Student eTool (CPM)

Use this eTool to help you solve each quadratic equation below by completing the square.
a. $x^{2} 6 x+7=0$
b. $p^{2}+2 p+1=0$
c. $k^{2} 4 k+9=0$

## Use the algebra tiles to represent the tiles.

1. Select one of the tiles and drag it to the tile area.
2. Use the sliders in the tray to change the size of the tiles.
3. Double click tiles to change orientation (horizontal/vertical).
4. Click on a tile once to change the sign (+ -).

Note: The color of the tile will turn to red for negative sign.


## Chapter 6

## INT2 6.2.3: 6-68 Student eTool (Desmos)

## Click on the link below to access eTool.

## 6-68 Student eTool (Desmos)

Use this eTool to help you determine where on the cabinet the sound system should be placed.

Move the slider below to find the shortest length of wire from the two speakers to the stereo.

- Click the BLUE point (slider) and drag horizontally to move.



## INT2 6.2.3: 6-68 Answer eTool (Desmos)

## Click on the link below to access eTool.

## 6-68 Answer eTool (Desmos)

## 6-68 Answer:

Move the slider along the x-axis (table top) to find the shortest length of wire from the two speakers to the sound system.

- Click the BLUE point and drag horizontally to move the slider.



## INT2 6.2.5: 6-90 Student eTool (CPM)

## Click on the link below to access eTool.

## 6-90 Teacher eTool (CPM)

## Use this eTool to complete the task in problem 6-90.

- Create a poster showing all four representations of this situation.
- On your poster, include a drawing of the pen with the largest possible area. State its dimensions (width and length) and its area.
- Use multiple representations to justify your conclusion that this is the largest pen.



## 1. Click the arrows on the left of 'Area and Perimeter' and 'General Tools' to view/

 hide the tools.
## 2. Click the tool to be used and drag it to the tile area.



## Chapter 7

## INT2 7.2.1: 7-67 Student eTool (CPM)

## Click on the link below to access eTool.

## 7-67 Student eTool (CPM)

Use this eTool to create a table for part (a) of problem 7-67.
Click on a cell and enter the value.

| Table <br> O 2016 CPM Educational Program. Al rights resenved. |  |  |  |  |  |  |  |  |  |  |  |  | Dircetions |  | beoct | savo |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1 | 2 |  | 4 |  | 6 |  |  |  |  |  |  |  |  |  |  |
| 1 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 2 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 3 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 4 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 5 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 6 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |

## Click on "Directions" for more information.



## INT2 7.2.1: 7-67 Answer eTool (CPM)

Click on the link below to access eTool.
7-67 Answer eTool (CPM)

## 7-67 Answer:



## Chapter 8

## INT2 8.2.1: 8-24 Student eTools (Desmos)

Click on the links below to access eTools.
8-24f1 Student eTool (Desmos)
8-24f2 Student eTool (Desmos)
8 -24f3 Student eTool (Desmos)
8-24f4 Student eTool (Desmos)
Use these eTools to help students confirm their conjectures about the exterior angles of various polygons.

With these eTools, students will notice that the sum of the exterior angles of a convex polygon will be $360^{\circ}$ regardless of whether or not the polygon is regular.

8-24f1: Exterior Angles - Triangles

1. Click the colored points and drag to change the triangle.
2. Click the BLUE point (slider) and drag horizontally to change the scale of exterior angles.


8-24f2: Exterior Angles - Quadrilaterals

1. Click the colored points and drag to change the quadrilateral.
2. Click the BLUE point (slider) and drag horizontally to change the scale of exterior angles.


## 8-24f3: Exterior Angles - Pentagons

1. Click the colored points and drag to change the pentagon.
2. Click the BLUE point (slider) and drag horizontally to change the scale of exterior angles.


8-24f4: Exterior Angles - Hexagons

1. Click the colored points and drag to change the hexagon.
2. Click the BLUE point (slider) and drag horizontally to change the scale of exterior angles.


## INT2 8.4.1: 8-79 Student eTool (Desmos)

## Click on the link below to access eTool.

8-79 Student eTool (Desmos)

## Use this eTool to explore the Area and Circumference of a Circle.

Click on the BLUE point (slider) and drag horizontally to change the length of the radius.


## Chapter 9

## INT2 9.1.2: 9-12 Student eTool (Desmos)

## Click on the link below to access eTool.

## 9-12 Student eTool (Desmos)

Use this eTool to complete the task in problem 9-12.


## INT2 9.3.4: 9-116 Student eTool (Desmos)

Click on the link below to access eTool.
9-116 Student eTool (Desmos)
Use this eTool to complete problems 9-116 and 9-117.


## INT2 9.3.4: 9-116 Answer eTool (Desmos)

## Click on the link below to access eTool.

## 9-116 Answer eTool (Desmos)

## 9-116 Answer:

Click on the circles to the left of lines 5, 7, and 9 to view/hide the graphs.


## Chapter 10

## INT2 10.1.1: 10-1 Student eTool (Desmos)

## Click the link below to access to eTool.

10-1 Student eTool (Desmos)

## Use this eTool to explore the equation of a circle.

## 1. Click the ORANGE point and drag to move.



## INT2 10.1.2: 10-15 Student eTool (CPM)

## Click on the link below to access eTool.

## 10-15 Student eTool (CPM)

Use the algebra tiles to help you rewrite the given equation below.

$$
x^{2}+y^{2}+4 x+2 y=11
$$

1. Click on each tile and drag to the desired location.


## INT2 10.1.3: 10-27 Student eTool (Desmos)

Click on the link below to access eTool.

## 10-27 Student eTool (Desmos)

This eTool is designed to move the focus and directrix of a parabola and observe the effect on the shape of the resulting parabola.

1. Click on the RED point (F) and drag up and down to see the distance between the focus and directrix affects the shape of the parabola.


## Chapter 11

## INT2 11.1.2: 11-16 Student eTool (CPM)

Click on the link below to access eTool.

## 11-16 Student eTool (CPM)

## Use this eTool to build 3D block solids.

1. Click on each square to add or remove blocks.

